



Comparison of the Economics and Performance of Horizontal and Vertical Wells

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Abstract: Horizontal wells generally have a better performance than vertical wells in terms of productivity, but are however more expensive to drill, complete and produce from. This work compares the performance of the two types of wells by estimating Productivity Index (PI) for horizontal and vertical wells under same reservoir parameters and determines which of the two types of wells is more economical. Joshi and Borisov's models for predicting horizontal Productivity Index are adopted in this research, while vertical Productivity Index is predicted using Joshi's model only. Economic evaluations of the two wells are done using investment decision criteria known as the Net Present Value (NPV). Hypothetical data used in all calculations generated results that indicated that horizontal wells have higher productivity than the vertical wells, and that the horizontal wells in this project are more economically acceptable than the vertical wells. In conclusion, Horizontal well Productivity Index increases with increasing horizontal well length while vertical productivity index is not affected by well length. Both horizontal and vertical productivity indices increase with increasing reservoir thickness. It is recommended that subsequent work in this field of study should consider productivity models that account for pseudo-steady state flow and reservoir anisotropy.

Keywords: Economics, Horizontal and Vertical wells, Net Present Value (NPV), Productivity Index, Well Performance

1. INTRODUCTION

During the initial stages of well planning, engineers will have to make the choice between drilling a vertical well or a horizontal well for a specific type of reservoir with unique properties that either types of drilling methods could favor. A reservoir with good height, thickness and a very large surface area will require a specific well type suitable to effectively drain it. Faced with this challenge, well planners, drilling engineers, production engineers and reservoir engineers have to make a choice on whether to drill several vertical wells on the location or to drill just one horizontal well to satisfactorily cover the reservoir area for effective drainage.

Several factors will affect the choice of the options available; some of which are; economics, information of reservoir characteristics from seismic surveys such as reservoir shape, height, length and dip angle of the reservoir, expected monetary returns on investment based on the productivity of the wells drilled, etc. Well performance is often measured in terms of the well's productivity which is dependent on a number factors such as the reservoir's configuration, the type of completion, petrophysical and fluid properties, formation damage, etc [1]. The productivity index of a well is a function of the pressure losses between the reservoir boundary and the well bore [2-5]. The factors that affect productivity index are reservoir drainage area, pay zone thickness, anisotropy, well length, fluid velocity, and well completion methods [6-8].

A vertical well is a well that is characterized by a generally vertical wellbore track. Because the risk of vertical well construction is relatively low, the techniques for drilling such a well are relatively simple and the maintenance of the subsequent oil extraction operation is relatively easy. Vertical well is the most widely used well type worldwide [9, 10]. In horizontal wells, the wellbore remains in high angle trajectory roughly parallel to the formation, thereby exposing significantly more attention zone

to production than would be exposed by a vertical well [11]. Productivity index for horizontal wells increases with well length, and anisotropy value; also horizontal wells are better suited for thin beds [12, 13]. This study seeks to determine the productivity and economic viability of a vertical and horizontal well for specific reservoir conditions in order to select the more suitable well type for the prevailing reservoir conditions.

2. MATERIALS AND METHODS

The model employed in this research to predict the productivity of the vertical wells was Joshi's method. Horizontal well productivity predictions in this project have been done by adopting two models which include Joshi's model and the Borisov's model. Reasonable reservoir, fluid, and well data were assumed for the prediction of both vertical and horizontal well productivity indices.

Net Present Value (NPV) is the commonest investment decision criteria used to assess the economic viability of an Exploration and Production (E&P) venture in today's market. It is one of the many criteria that takes into account the time value of money and is relatively simpler to use than other decision criteria.

2.1. Horizontal Productivity Models

Borisov's Model

Borisov in 1984 proposed the following expression for predicting the productivity index of a horizontal well in an isotropic reservoir [14], i.e., $k_v = k_h$

$$J_h = \frac{0.00708hk_h}{\mu_o B_o \left[\ln\left(\frac{4r_{eh}}{L}\right) + \left(\frac{h}{L}\right) \ln\left(\frac{h}{2\pi r_w}\right) \right]} \quad (1)$$

Where, J_h = horizontal productivity index, STB/day/psi

kh = horizontal permeability, md

h = thickness, ft.

L = well length

B_o = oil formation volume factor, bbl/STB

μ_o = oil viscosity, cp.

r_{eh} = drainage radius, ft.

r_w = wellbore radius, ft

Joshi's Model

Joshi in 1991 presented the following expression for estimating the productivity index of a horizontal well in isotropic reservoirs [15]. Joshi accounted for the influence of the reservoir anisotropy by introducing the vertical permeability k_v into his equation.

$$J_h = \frac{0.00708hk_h}{\mu_o B_o \left[\ln(R) + \left(\frac{B^2h}{L}\right) \ln\left(\frac{h}{2r_w}\right) \right]} \quad (2)$$

Where, J_h = horizontal productivity index, STB/day/psi

kh = horizontal permeability, md

h = thickness, ft.

L = well length

B_o = oil formation volume factor, bbl/STB

μ_o = oil viscosity, cp.

r_w = wellbore radius, ft

The parameters R and B are represented by the equations below,

$$R = \frac{a + \sqrt{a^2 - (L/2)^2}}{(L/2)} \tag{3}$$

Where, L = well length

a = half the major axis of drainage of the ellipse and expressed by the equation below.

$$a = \left(\frac{L}{2}\right) \left[0.5 + \sqrt{0.25 + (2r_{eh}/L)^4}\right]^{0.5} \tag{4}$$

$$B = \sqrt{\frac{k_h}{k_v}} \tag{5}$$

Where, k_h = horizontal permeability, md

k_v = vertical permeability, md

r_{eh} = drainage radius, ft.

Joshi’s Method for Drainage Area

Figure 1 shows the drainage areas for a vertical well (Fig 1a) and a horizontal well (Fig. 1b). A vertical well drains a cylindrical volume as illustrated while a horizontal well drains an ellipsoid. It is generally expected that a horizontal well drains a larger volume than a vertical well [15].

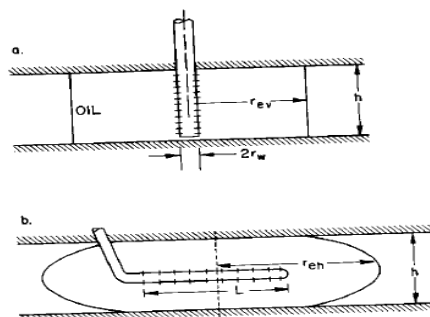


Figure1. A Schematic of a Vertical and Horizontal Well Drainage Area (Joshi, 1991)

A horizontal well can be looked upon as a number of vertical wells drilling next to each other and completed in a limited pay zone thickness. Figure 2 below shows the drainage area of a horizontal well of length (L) in a reservoir with a pay zone thickness (h). Each end of the horizontal well would drain a half-circular area of radius b, with a rectangular drainage shape of the horizontal well [16].

Joshi (1991) assumed that each end of the horizontal well is represented by a vertical well that drains an area of a half circle with a radius of b. He therefore proposed the following two methods for calculating the drainage area of a horizontal well.

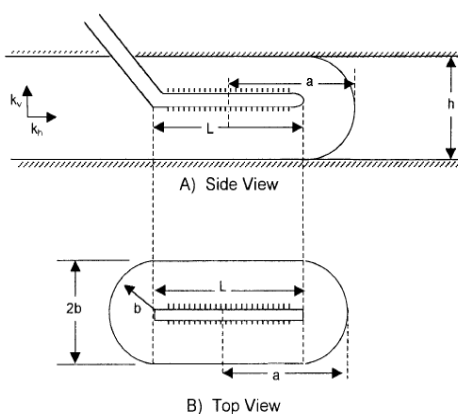


Figure2. Schematic of a Horizontal Well Drainage Area (Tarek, 2006)

Method 1: Under this method, Joshi proposed that the drainage area is represented by two half circles of radius b (equivalent to a radius of a vertical well rev) at each end and a rectangle, of dimensions L ($2b$), in the center. The drainage area is therefore represented by the equation below.

$$A = \frac{L(2b) + \pi b^2}{43560} \quad (6)$$

Where, A = drainage area, acres

L = length of horizontal well, ft.

b = half minor axis of an ellipse, ft.

Method 2: In method 2, Joshi assumed that total horizontal drainage area is an ellipse and is represented by the equation below.

$$A = \frac{\pi ab}{435600} \quad (7)$$

Where, A = drainage area

a = major axis of an ellipse also represented mathematically as shown below

$$a = \frac{L}{2} + b \quad (8)$$

Where, L = well length, ft.

b = half minor axis of an ellipse, ft.

Joshi noted that the two methods give different values for the drainage area A and suggested assigning the average value for the drainage of the horizontal well.

Most methods used to predict productivity index of horizontal wells usually require a parameter known as drainage radius. The drainage radius of a well is represented mathematically as shown below

$$r_{eh} = \sqrt{\frac{43560A}{\pi}} \quad (9)$$

Where, r_{eh} = drainage radius, ft.

A = reservoir area, acres

2.2. Vertical Well Productivity

Ideally bottom hole flowing pressure (P_{wf}) for at a certain flow rate (q) is measured using a bottomhole pressure gauge. A build up or drawdown test is used to estimate the average reservoir pressure (P_r) along with other parameters such as skin factor (s). Flow rate of a well producing under steady-state radial flow is given by:

$$Q_o = \frac{0.00708K_o h(P_r - P_{wf})}{\mu_o B_o \left[\ln\left(\frac{r_e}{r_w}\right) + S \right]} \quad (10)$$

Where, Q_o = oil flow rate, STB/day

k = permeability, md

h = thickness, ft.

s = skin factor

B_o = oil formation volume factor, bbl/STB

μ_o = oil viscosity, cp.

P_i = initial reservoir pressure, psi

P_{wf} = bottom hole flowing pressure, psi

r_e = reservoir radius, ft.

r_w = wellbore radius, ft.

The productivity index of well can therefore be expressed as below:

$$J = \frac{0.00708k_h}{\mu_o B_o \left[\ln \left(\frac{r_e}{r_w} \right) + S \right]} \quad (11)$$

Where, J = productivity index (STB/day/psi)

k_h = horizontal permeability (md)

μ_o = oil viscosity (cp)

B_o = oil formation volume factor, bbl/STB

r_e = reservoir radius, ft.

r_w = wellbore radius, ft

S = skin factor

The skin factor is denoted by ‘S’, and is expressed as;

$$S = \left[\frac{k}{k_{skin}} - 1 \right] \ln \left(\frac{r_{skin}}{r_w} \right) \quad (12)$$

Where, S = skin factor

k = reservoir permeability, md

k_{skin} = permeability of damaged zone, md

r_{skin} = radius of damaged zone, ft

r_w = wellbore radius, ft

2.3.NPV Calculation for the Horizontal and Vertical Well

Using the productivity index value from Borisov’s model with the well length of 1000 ft and reservoir thickness of 160 ft, the net present value was calculated. Formulae used;

$$d = 1 - \exp(-a) \quad (13)$$

Where, d = rate of decline

a = effective annual decline

$$a = \left[\ln \left(\frac{q_i}{q_o} \right) \right] / t \quad (14)$$

Where, a = rate of buildup

q_i = initial production, bbl/day.

q_o = production at time t, bbl/day.

t = time, years.

$$q_t = q_i (e^{-at}) \quad (15)$$

Where, q_t = flow rate a certain time, bbl/day

q_i = initial flow rate, bbl/day

a = buildup rate

t = time, years.

$$N_p = \left(\frac{1}{a}\right)(q_i - q_o)(1/t) \tag{16}$$

Where, Np = production for a period

a = buildup

qi = initial flow rate, bbl/day

qo = production at time t, bbl/day.

t = time, years.

Equations 2.8 to equation 2.11 above are the equations used for production forecasting to aid in the calculation of the net present value. The equation below is the summary of the definition of Net Present Value and served as a guiding principle for all the NPV calculations in this project.

$$NPV = \sum PV_{\text{of cash inflow @i}^*} - \sum PV_{\text{of cash outflow @i}^*} \tag{17}$$

Where, NPV = Net Present Value

PV = Present Value

i* = minimum rate of return

3. RESULTS AND DISCUSSION

3.1. Results

All hypothetical parameters that were used for productivity index calculations and all related calculations are displayed in Table 1. The productivity of the wells was calculated using Microsoft Excel software. The results of productivity index using Borisov and Joshi’s models are summarized in Table 2 and Table 3 respectively. Figure 3 is a graph representing such a plot thus productivity ratio against well length.

The Tables 4 and 5 are a summary of computations of productivity index using Borisov and Joshi’s models respectively. The resulting productivity indices were then plotted against the corresponding reservoir thickness as shown in Figure 4 below. Assumed data for all calculations of the Net present value done are displayed in table 6 below. The table 7, table 8, and table 9 shows summary of the calculations of net present value.

Table1. Parameters for Calculation of Productivity Index

Reservoir data		Fluid data		Well data	
Vertical Permeability, K _v	75 md	Oil viscosity	0.62 cp	Well length, L	1000 ft
Horizontal Permeability, K _h	75 md	Oil formation volume factor, B _o	1.35 bbl/STB	Wellbore radius, r _w	0.365 ft
Reservoir thickness, h	160 ft			Reservoir radius, r _e	1053 ft
Porosity, φ	3.8 %			Area, A	80 acres
				Skin zone radius, r _s	1.312 ft
				Permeability of skin zone, k _{skin}	5.894 md

Table2. Summary of Computations Using Borisov’s Model

Well length of horizontal section, ft.	250	500	750	1000	1250	1500	1750	2000
Horizontal well productivity index, STB/day/psi (Borisov's Model)	18.32	29.09	38.57	47.94	57.73	68.33	80.14	93.59
Vertical Productivity index, STB/day/psi	11.56	11.56	11.56	11.56	11.56	11.56	11.56	11.56
Productivity ratio	1.58	2.52	3.34	4.15	4.99	5.91	6.93	8.09

Table3. Summary of Computations Using Joshi’s Model

Well length of horizontal section, ft.	250	500	750	1000	1250	1500	1750	2000
Horizontal well productivity index, STB/day/psi (Joshi's Model)	16.18	26.32	35.29	44.09	53.18	62.83	73.26	84.60
Vertical Productivity index, STB/day/psi	11.56	11.56	11.56	11.56	11.56	11.56	11.56	11.56
Productivity ratio	1.40	2.28	3.05	3.81	4.60	5.43	6.34	7.32

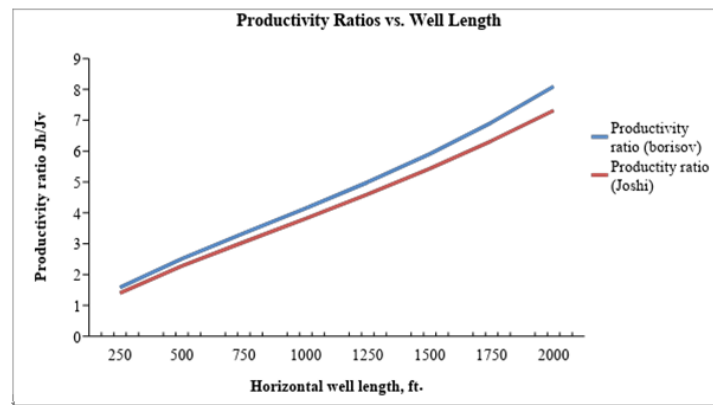


Figure3. Productivity Ratios Vs. Well Length

Table4. Productivity Index Values for Varying Reservoir Thickness

Reservoir Thickness	Productivity Index (Borisov's Model)	Vertical Productivity Index
40	16.35	2.89
50	19.92	3.61
60	23.30	4.34
70	26.47	5.06
80	29.47	5.78
90	32.29	6.50
100	34.94	7.23
110	37.44	7.95
120	39.79	8.67
130	42.01	9.39
140	44.11	10.12
150	46.08	10.84
160	47.94	11.56

Table5. Productivity Index Values for Varying Reservoir Thickness

Reservoir Thickness	Productivity Index (Joshi's Model)	Vertical Productivity Index
40	15.86	2.89
50	19.21	3.61
60	22.33	4.34
70	25.24	5.06
80	27.96	5.78
90	30.48	6.50
100	32.84	7.23
110	35.04	7.95
120	37.10	8.67
130	39.02	9.39
140	40.82	10.12
150	42.51	10.84
160	44.09	11.56

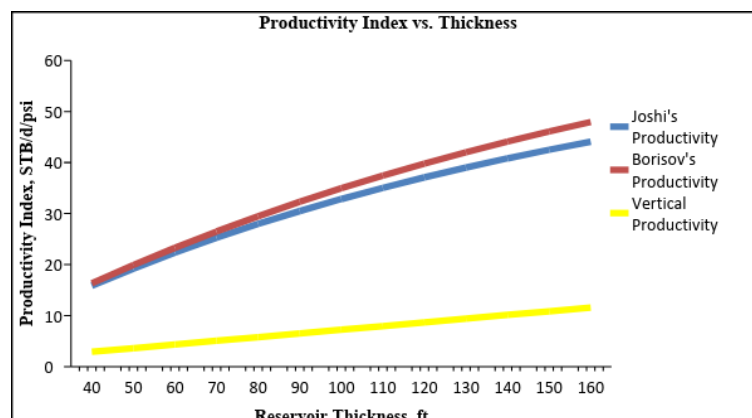


Figure4. Productivity Index versus Thickness

Table6. Hypothetical Data for NPV Calculation

Parameter	Value	Units
Annual decline rate	10	%
Discount rate of return	15	%
Opex/year	15,000,000	\$
Peak production horizontal well	5000	bbl/day
Exploration cost	100,000,000	\$
Development cost (vertical well)	65,000,000	\$
Development cost (horizontal well)	110,000,000	\$
Tax Percentage	30	%
Royalty	12	%
Peak production vertical well	2900	bbl/day
Initial pressure	2850	Psi
Well bore pressure	2790	Psi

Table7. Horizontal Well Economic Evaluation (Borisov)

Time	Instantaneous Production Bopd	Yearly Production (STB/year)	Gross Revenue (\$)	Royalty (\$)	Net Revenue (\$)	CAPEX (\$)	OPEX (\$)	Taxable Income (\$)	30% Tax (\$)	Government Take (\$)	Operator Take (\$)
2014	2876.38	1209349.25	133,028,417.29	15,963,410.07	117,065,007.21	50,000,000.00	10,000,000.00	57,065,007.21	17,119,502.16	33,082,912.24	39,945,505.05
2015	3792.35	1594460.97	175,390,707.20	21,046,884.86	154,343,822.34	50,000,000.00	10,000,000.00	94,343,822.34	28,303,146.70	49,350,031.57	66,040,675.64
2016	5000.00	1825000.00	200,750,000.00	24,090,000.00	176,660,000.00	65,000,000.00	10,000,000.00	101,660,000.00	30,498,000.00	54,588,000.00	71,162,000.00
2017	4500.00	1558933.14	171,482,645.92	20,577,917.51	150,904,728.41	45,000,000.00	10,000,000.00	95,904,728.41	28,771,418.52	49,349,336.03	67,133,309.88
2018	4050.00	1403039.83	154,334,381.32	18,520,125.76	135,814,255.56		10,000,000.00	125,814,255.56	37,744,276.67	56,264,402.43	88,069,978.90
2019	3645.00	1262735.85	138,900,943.19	16,668,113.18	122,232,830.01		10,000,000.00	112,232,830.01	33,669,849.00	50,337,962.19	78,562,981.01
2020	3280.50	1136462.26	125,010,848.87	15,001,301.86	110,009,547.01		10,000,000.00	100,009,547.01	30,002,864.10	45,004,165.97	70,006,682.91
2021	2952.45	1022816.036	1,125,097,639.85	135,011,716.78	990,085,923.07		10,000,000.00	980,085,923.07	294,025,776.92	429,037,493.70	686,060,146.15
Total			2,223,995,583.64					NPV (Operator)			498,188,991.57
								NPV (Government)			337,099,296

Table8. Horizontal Well Economic Evaluation (Joshi)

Time	Instantaneous Production Bopd	Yearly Production (STB/year)	Gross Revenue (\$)	Royalty (\$)	Net Revenue (\$)	CAPEX (\$)	OPEX (\$)	Taxable Income (\$)	30% Tax (\$)	Government Take (\$)	Operator's Take (\$)
2014	2645.56	1112302.43	122,353,267.27	14,682,392.07	107,670,875.20	50,000,000	10,000,000	47,670,875.20	14,301,262.56	28,983,654.63	33,369,612.64
2015	3488.02	1996259.61	219,588,556.64	26,350,626.80	193,237,929.84	50,000,000	10,000,000	133,237,929.84	39,971,378.95	66,322,005.75	93,266,550.89
2016	5000.00	1825000.00	200,750,000.00	24,090,000.00	176,660,000.00	65,000,000	10,000,000	101,660,000.00	30,498,000.00	54,588,000.00	71,162,000.00

Comparison of the Economics and Performance of Horizontal and Vertical Wells

2017	4500.00	155893 3.14	171,48 2,645. 92	20,577, 917.51	150,904, 728.41	45,00 0,000	10,000 ,000	95,904,7 28.41	28,771 ,418.5 2	49,349, 336.03	67,133 ,309.8 8
2018	4050.00	140303 9.83	154,33 4,381. 32	18,520, 125.76	135,814, 255.56		10,000 ,000	125,814, 255.56	37,744 ,276.6 7	56,264, 402.43	88,069 ,978.9 0
2019	3645.00	126273 5.85	138,90 0,943. 19	16,668, 113.18	122,232, 830.01		10,000 ,000	112,232, 830.01	33,669 ,849.0 0	50,337, 962.19	78,562 ,981.0 1
2020	3280.50	113646 2.26	125,01 0,848. 87	15,001, 301.86	110,009, 547.01		10,000 ,000	100,009, 547.01	30,002 ,864.1 0	45,004, 165.97	70,006 ,682.9 1
2021	2952.45	102281 60.36	1,125, 097,63 9	135,011 ,716	990,085, 923.07		10,000 ,000	980,085, 923.07	294,02 5,776. 92	429,03 7,493.7 0	686,06 0,146. 15
Total			2,257, 518,28 3.06						NPV (Operator)		513,05 7,497. 42
									NPV (Government)		346,36 7,974. 49

Table9. Economics of a Vertical Well

Time	Instantaneous Production Bopd	Yearly Production (STB/year)	Gross Revenue (\$)	Royalty (\$)	Net Revenue (\$)	CAP EX (\$)	OPEX (\$)	Taxable Income (\$)	30% Tax (\$)	Government Take (\$)	Operator's Take (\$)
2014	693.76	956759. 99	105,24 3,598. 68	12,629 ,231.8 4	92,614, 366.84	50,00 0,000	10,00 0,000	32,614,3 66.84	9,784,31 0.05	22,413,5 41.89	22,830 ,056.7 9
2015	1418.42	195612 2.07	215,17 3,428. 21	25,820 ,811.3 9	189,352 ,616.82	50,00 0,000	10,00 0,000	129,352, 616.82	38,805,7 85.05	64,626,5 96.43	90,546 ,831.7 8
2016	2900.00	105850 0.00	116,43 5,000. 00	13,972 ,200.0 0	102,462 ,800.00	35,00 0,000	10,00 0,000	57,462,8 00.00	17,238,8 40.00	31,211,0 40.00	40,223 ,960.0 0
2017	2610.00	904181. 22	99,459 ,934.6 3	11,935 ,192.1 6	87,524, 742.48	30,00 0,000	10,00 0,000	47,524,7 42.48	14,257,4 22.74	26,192,6 14.90	33,267 ,319.7 3
2018	2349.00	813763. 10	89,513 ,941.1 7	10,741 ,672.9 4	78,772, 268.23		10,00 0,000	68,772,2 68.23	20,631,6 80.47	31,373,3 53.41	48,140 ,587.7 6
2019	2114.10	732386. 79	80,562 ,547.0 5	9,667, 505.65	70,895, 041.40		10,00 0,000	60,895,0 41.40	18,268,5 12.42	27,936,0 18.07	42,626 ,528.9 8
2020	1902.69	659148. 11	72,506 ,292.3 5	8,700, 755.08	63,805, 537.26		10,00 0,000	53,805,5 37.26	16,141,6 61.18	24,842,4 16.26	37,663 ,876.0 9
2021	1712.42	593233 3.01	652,55 6,631. 11	78,306 ,795.7 3	574,249 ,835.38		10,00 0,000	564,249, 835.38	169,274, 950.6	247,581, 746.35	394,97 4,884. 77
Total			1,431, 451,37 3.2						NPV (Operator)		319,42 7,483. 00
									NPV (Government)		\$221,8 04,215 .5

3.2. Discussion

3.2.1. Effects of Well Length on Horizontal Productivity

The results of productivity index using Borisov and Joshi's models are summarized in Table 2 and Table 3 respectively. All calculations were done using Microsoft Excel software.

The different values of calculated productivity ratios from two different horizontal well productivity models were plotted against varying well lengths of the perforated horizontal section. Figure 3 is a graph representing such a plot.

It can be observed from the graph that the productivity index of horizontal wells increases as the length of the perforated horizontal section of the well is increased. A length of 250 ft registers a

productivity ratio of 1.58 and 1.40 from Borisov and Joshi's model respectively. A length of 750 ft, 1250 ft, and 2000 ft registered productivity ratios of 3.34, 4.99, and 8.09 respectively for Borisov's model and 3.05, 4.60, and 7.32 respectively for Joshi's model.

No change was observed in the productivity index of a vertical well calculated using Joshi's model. The vertical well productivity index was calculated to be 11.56 STB/day/psi using Joshi's model for vertical productivity index. The vertical productivity remained 11.56 STB/day/psi because the well length (L) parameter is not accounted for in Joshi's equation for vertical productivity.

3.2.2. *Effects of Reservoir Thickness on well Productivity*

The parameter of reservoir thickness (h) was varied in the various equations for calculation of productivity index, starting from 40 ft. to 160 ft. while maintaining a horizontal well length section of 1000 ft. Both horizontal and vertical productivity indices were observed to increase with increasing reservoir thickness. Table 4 and table 5 are summaries of the calculations involving variations in reservoir thickness.

The vertical productivity index was calculated to be 2.89 STB/day/psi, 5.78 STB/day/psi, 8.67 STB/day/psi, and 11.56 STB/day/psi at reservoir thickness of 40 ft, 80 ft, 120 ft, and 160 ft respectively. Using Borisov's model, productivity index values of 16.35 STB/day/psi, 29.47 STB/day/psi, 39.79 STB/day/psi, and 47.94 STB/day/psi were calculated with corresponding reservoir thicknesses of 40 ft, 80 ft, 120 ft, and 160 ft respectively.

Productivity index values of 15.86 STB/day/psi, 27.96 STB/day/psi, 37.10 STB/day/psi, and 44.09 STB/day/psi were calculated using Joshi's model with corresponding reservoir thickness of 40 ft, 80 ft, 120 ft, and 160 ft respectively. A graph of productivity index against reservoir thickness was plotted in figure 3.4 to show graphical representations of how reservoir thickness affects productivity.

3.2.3. *Net Present Value*

A summary of the net present value calculations are shown in table 3.7, table 3.8 and table 3.9. From Table 3.7, the Net Present Value of the operator's take of the horizontal well using Borisov's horizontal productivity index for production forecast was \$498,188,991.57, while the Net Present Value of the government's take was \$337,099,296.

The Net Present Value of the operator's take from the horizontal well using Joshi's productivity index for production forecast was \$513,057,497.42, while the Net Present Value of government's take was \$346,367,974.49.

Using the vertical productivity index to forecast production from the vertical well, a Net Present Value of \$319,427,483.00 was calculated from the operator's take, while a Net Present Value Of \$221,804,215.51 was calculated from the government's take.

It is therefore evident that the horizontal wells in this project are more economical to both the operator and the host government than the vertical well.

4. CONCLUSION

The following conclusions can be drawn from this study;

- Horizontal wells have a higher productivity than a conventional vertical well.
- Horizontal well productivity index increases with increasing horizontal well length while vertical productivity index is not affected by well length.
- Both horizontal and vertical productivity indices increase with increasing reservoir thickness.
- Sinking a horizontal well in this case is more economical than sinking a vertical well as its net present value is greater than the net present value of a vertical well.

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