

Unification for Gravity and Electromagnetic Field in Kerr Newman Solution

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Abstract: Solutions of unified theory equations of gravity and electromagnetism has to satisfy Einstein-Maxwell equation. Specially, solution of the unified theory is generally Kerr-Newman solution in vacuum. We finally found the revised Einstein gravity tensor equation with new term (2-order contravariant metric tensor two times product and the constant matrix) is right in Kerr-Newman solution.

Keywords: General relativity theory, Unified Theory; Kerr-Newman solution; 2-order contravariant metric tensor two times product; The constant matrix

PACS Number: 04,04.90.+e,41.12

1. INTRODUCTION

This theory's aim is that we discover the revised Einstein gravity equation had Kerr-Newman solution in vacuum.

First, we know the revised Einstein gravity equation[1].

$$R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R + \Lambda g_{\mu\nu}I(g^{\theta\theta})^2 = -\frac{8\pi G}{c^4}T_{\mu\nu}$$

In this time,

$$\Lambda = k \frac{GQ^2}{c^4}, I = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix} \quad (1)$$

If Eq(1) take covariant differential operator,

$$(R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R)_{;\mu} + \Lambda g_{\mu\nu}I_2 g^{\theta\theta} g^{\theta\theta}_{;\mu} = -\frac{8\pi G}{c^4}T_{\mu\nu;\mu} = 0 \quad (2-i)$$

$$(R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R)_{;\nu} + \Lambda g_{\mu\nu}I_2 g^{\theta\theta} g^{\theta\theta}_{;\nu} = -\frac{8\pi G}{c^4}T_{\mu\nu;\nu} = 0 \quad (2-ii)$$

In this time, in Kerr-Newman solution

$$\begin{aligned} g_{\theta\theta} &= 1/g^{\theta\theta} = \rho^2 = r^2 + a^2 \cos^2 \theta \\ g^{\theta\theta}_{;\rho} &= \frac{\partial g^{\theta\theta}}{\partial x^\rho} + 2\Gamma^{\theta}_{\sigma\rho} g^{\sigma\theta} = \frac{\partial g^{\theta\theta}}{\partial r} + 2\Gamma^{\theta}_{0r} g^{\theta\theta} \\ &= \frac{\partial}{\partial r} \left(\frac{1}{\rho^2} \right) + 2 \cdot \frac{r}{\rho^2} \cdot \frac{1}{\rho^2} = -2 \frac{1}{\rho^3} \cdot \frac{r}{\rho} + \frac{2r}{\rho^4} = 0 \\ g^{\theta\theta}_{;\theta} &= \frac{\partial g^{\theta\theta}}{\partial x^\theta} + 2\Gamma^{\theta}_{\sigma\theta} g^{\sigma\theta} = \frac{\partial g^{\theta\theta}}{\partial \theta} + 2\Gamma^{\theta}_{\theta\theta} g^{\theta\theta} \\ &= \frac{\partial}{\partial \theta} \left(\frac{1}{\rho^2} \right) - 2 \cdot \frac{1}{\rho^2} \cdot \frac{1}{2} \rho \frac{2a^2}{\rho} \cos \theta \sin \theta \cdot \frac{1}{\rho^2} \end{aligned} \quad (3)$$

$$= -2 \cdot \frac{1}{\rho^3} \cdot -\frac{2a^2 \cos\theta \sin\theta}{\rho} - \frac{4a^2}{\rho^4} \cos\theta \sin\theta = 0 \tag{4}$$

If $g^{\theta\theta}_{;\rho} = V_\rho$, the vector transformation is

$$0 = V_\rho = \frac{\partial x^\alpha}{\partial x^\rho} V'_\alpha, V'_\alpha = 0 \tag{5}$$

Therefore, if the coordinate is not the Kerr-Newman's coordinate, the covariant differential of

$$g^{\theta\theta} = \frac{1}{\rho^2} \text{ is still zero in the changed coordinates.}$$

2. THE REVISED EINSTEIN GRAVITY EQUATION AND KERR-NEWMAN SOLUTION

In this theory, Eq(1) can change the following equation.

$$R_{\mu\nu} = -\frac{8\pi G}{c^4} (T_{\mu\nu} - \frac{1}{2} g_{\mu\nu} T^\lambda{}_\lambda) + \Lambda g_{\mu\nu} I(g^{\theta\theta})^2 \tag{6}$$

In this time, in vacuum, specially, in Kerr-Newman solution,

$$T_{\mu\nu} = 0, T^\lambda{}_\lambda = g^{\mu\nu} T_{\mu\nu} \neq 0 \tag{7}$$

Therefore, Eq(1) is

$$\begin{aligned} T_{\mu\nu} = 0, -\Lambda g_{\mu\nu} I(g^{\theta\theta})^2 &= R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R = \frac{2G}{c^5} (F_{\mu\rho} F_{\nu}{}^\rho - \frac{1}{4} g_{\mu\nu} F_{\rho\sigma} F^{\rho\sigma}) \\ &= \frac{2G}{c^5} (g_{\mu\nu} F_{\nu\rho} F^{\nu\rho} - \frac{1}{4} g_{\mu\nu} F_{\rho\sigma} F^{\rho\sigma}) \end{aligned} \tag{8}$$

In this time, According to [2],

$$\begin{aligned} E = F_{01} = -F_{10} &= \frac{Q (r^2 - a^2 \cos^2 \theta)}{(r^2 + a^2 \cos^2 \theta)^2} = \frac{Q (r^2 - a^2 \cos^2 \theta)}{\rho^4} \\ B = F_{23} = -F_{32} &= \frac{2Q \arccos \theta}{(r^2 + a^2 \cos^2 \theta)^2} = \frac{2Q \arccos \theta}{\rho^4} \end{aligned} \tag{9}$$

Hence,

$$\begin{aligned} &\frac{2G}{c^5} (g_{\mu\nu} F_{\nu\rho} F^{\nu\rho} - \frac{1}{4} g_{\mu\nu} F_{\rho\sigma} F^{\rho\sigma}) \\ &= -\frac{G}{c^5} g_{\mu\nu} I(B^2 + E^2), I = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix} \\ &= -\frac{G}{c^5} \begin{pmatrix} g_{00} & 0 & 0 & -g_{03} \\ 0 & g_{11} & 0 & 0 \\ 0 & 0 & -g_{22} & 0 \\ g_{30} & 0 & 0 & -g_{33} \end{pmatrix} (B^2 + E^2), B^2 + E^2 = \frac{Q^2}{\rho^4} \\ &= -\frac{G}{c^5} \begin{pmatrix} g_{00} & 0 & 0 & -g_{03} \\ 0 & g_{11} & 0 & 0 \\ 0 & 0 & -g_{22} & 0 \\ g_{30} & 0 & 0 & -g_{33} \end{pmatrix} \frac{Q^2}{\rho^4} = -\Lambda g_{\mu\nu} I(g^{\theta\theta})^2 \end{aligned}$$

$$\Lambda = k \frac{GQ^2}{c^4} \quad (10)$$

3. CONCLUSION

We finally found the revised Einstein equation of unified theory (the gravity and electromagnetic field) is right in Kerr-Newman solution.

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Citation: Sangwha-Yi, (2019). Unification for Gravity and Electromagnetic Field in Kerr-Newman Solution. *International Journal of Advanced Research in Physical Science (IJARPS)* 6(12), pp.11-13, 2019.

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