# Excess Free Volumes, Internal Pressures and Molar Available Volumes in the Binary Liquid Mixtures of N-Methyl-2-Pyrrolidone at Different Temperatures

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**Abstract:** Available volume, molar free volume, internal pressure and their excess values are determined from the measured data of ultrasonic speeds, densities and viscosities of binary fluid mixtures of N-methyl-2-pyrrolidone (NMP) and Propyl amine (PA) or Butylamine (BA) or Dipropylamine (DPA) at different temperatures with an interval of 5 K from 303.15 to 318.15 K. Excess properties are fitted to a Redlich–Kister type equation. The excess available volume and excess molar free volumes are found to be negative where as the excess internal pressures are found to be positive. The results observed from these studies suggest dipole-dipole and Hydrogen-bonded interactions between unlike molecules in all the three systems investigated.

**Keywords:** Density, viscosity, speeds of sound, Thermo acoustic properties, Relich-Kister polynomial, molecular interactions.

## **1. INTRODUCTION**

The knowledge on variation of thermodynamic properties with temperature involving non electrolyte solutions is of substantial significance in the chemical industry connecting chemical separations, mass transfer, fluid flow and heat transfer. When two or more solvent molecules are associated with one another to form a liquid mixture, it brings about a marked effect on the intermolecular interactions, due to changes in free volume, energy and molecular orientations leading to corresponding variations in the thermodynamic properties. In recent years, ultrasonic technique has become a powerful tool in providing information regarding the molecular behavior of liquids and solids owing to its ability of characterizing physiochemical behavior of the medium. The present work is a continuation of our research programme on thermodynamic, thermo-acoustic and transport behaviour of binary liquid mixtures of industrially important components [1-6].

Lactams are significant class of amides not extensively studied despite their use as solvents and biological applications. Hence, one of the lactams, N-methyl-2-Pyrrolidone (NMP) is chosen as a common solvent for the present study. NMP known for its solvent power is rapidly becoming the product of choice for paint strippers, agricultural chemicals, and process solvent applications [7-10]. In this paper we report the internal pressures, free volumes and molar available volumes of the binary systems N-methyl-2-Pyrrolidone (NMP) + propylamine (PA) or Butylamine (BA) or Dipropylamine (DPA) at temperatures 303.15 - 318.15 K.

## **2. EXPERIMENTAL SECTION**

The chemicals, NMP (>99%) obtained from Merck and Propylamine (>99%), Butylamine (>99%), Dipropylamine (>99%) procured from S.D. Fine chemicals (India) are further purified by using standard methods [9]. The purity of the chemicals was assessed by comparing their

measured densities ( $\rho$ ), ultrasonic velocities (U) and viscosities ( $\eta$ ), which are in good agreement with literature [11-15] values as can be seen in Table 1. The binary mixtures have been prepared gravimetrically using an electronic balance (Shimadzu AY 120, Japan) with an uncertainty of  $\pm$ 1x 10<sup>-7</sup> Kg and are stored in air-tight glass bottles. The densities,  $\rho$ , of pure liquids and their mixtures are determined using a 10<sup>-5</sup> m<sup>3</sup> double-arm pycnometer as described by Nikam et al [16]. The density values from triplicate replication at each temperature are accurate unto 4 parts in 10<sup>5</sup> parts. The ultrasonic velocity of pure components and their mixtures have been measured by single crystal variable path fixed frequency interferometer provided by Mittal Enterprises, New Delhi (Model-F 05). The measured speeds of sound are found to be accurate up to 0.1 m·s<sup>-1</sup>. Temperature control for the measurement of viscosity, density and ultrasonic velocity is achieved by using a microprocessor assisted circulating water bath, (supplied by Mac, New Delhi) regulated to ±0.01 K, using a proportional temperature controller.

**Table1.** Comparison of experimental values of density ( $\rho$ ), and ultrasonic speed (U) of pure liquids with the corresponding literature values at 303.15 K

	10	$^{-3} \mathrm{x}\rho (\mathrm{kg}\mathrm{m}^{-3})$	$U (\mathrm{m \ s}^{-1})$			
Liquid	Expt	Lit.	Expt	Lit.		
N-methyl-2-pyrrolidone	1.0238	1.02376 [11]	1552.8	1552 [12]		
Propylamine	0.7093	0.70927 [13]	1193.1	1193.96 [13]		
Butylamine	0.7289	0.72842 [14]	1226.0	1227 [14]		
Dipropylamine	0.7316	0.73133 [13]	1175.0	1174 [15]		

### 3. RESULTS AND DISCUSSION

Assuming that ultrasonic absorption is negligible, using experimental results of density, viscosity and ultrasonic velocity, the thermodynamic and thermoacoustic parameters such as free volume  $(V_f)$ , internal pressure  $(\pi_i)$ , molar available volume  $(V_a)$  and their excess parameters have been calculated using the following standard expressions and are presented in Tables 2-4.

Erying et al [17] obtained the relationship between the internal pressure  $P_i$ , the external pressure P and the free volume  $V_f$  of a liquid as follows:

$$V_f = [KRT/(P_i+P) (\rho + V_f^{1/3}/K)^2]^3$$

The above relationship shows that free volume of a molecule at a particular temperature and pressure depends only on the internal pressure of the liquid in which it is immersed. The free volumes of the binary mixtures have been computed using its relationship with the ultrasonic velocity and viscosity as follows:

$$V_f = \left[\frac{M_{eff}U}{K\eta}\right]^{3/2} \tag{1}$$

where 'K' (=  $4.28 \times 10^9$  in S. I system) is a temperature independent proportionality constant and the other symbols have their usual meaning.

Suryanarayana and Kuppuswami [18] used an indirect alternative method for computing the internal pressure of a liquid from its viscosity, density and ultrasonic velocity as shown below

$$\pi_i = bRT \left[\frac{K\eta}{U}\right]^{1/2} \left[\frac{\rho^{2/3}}{M^{7/6}}\right]$$
(2)

where 'b' is a packing factor, 'R' is Universal gas constant, 'T' is the absolute temperature and other symbols have their usual meaning.

The molar available volume is the parameter related molecular interactions of the medium and calculated by using the expression

$$V_a = V_m \left( 1 - \frac{U}{U_{\infty}} \right) \tag{3}$$

The excess properties such as  $V_f^E$ ,  $V_a^E$  and  $\pi_i^E$  have been calculated using the equation  $Y^E = Y_{mix} - (x_1Y_1 + x_2Y_2)$  (4)

where  $Y^E$  is  $V_f^E$  or  $V_a^E$  or  $\pi_i^E$  and  $x_1$  and  $x_2$  are mole fractions of liquid 1 and 2 respectively.

These excess functions are fitted to Redlich – Kister [19] type polynomial equation.  $Y_{cal}^{E} = x_{1}x_{2}\sum a_{j-1}(x_{2}-x_{1})^{j-1}$ (5)

The values of coefficient  $a_{j-1}$  are evaluated by the method of least squares with all points weighed equally and the standard deviations are calculated using

$$\sigma_{YE} = \left[\frac{\Sigma(Y_{obs}^{E} - Y_{cal}^{E})^{2}}{(m-n)}\right]^{1/2}$$
(6)

where 'm' is the number of experimental data points and 'n' is the number of coefficients considered (n = 5 in the present calculation).

It is evident from Tables 2-4, that all the three binary systems exhibit non-linear increase/decrease in  $V_{\rm f}$ ,  $V_{\rm a}$  and  $\pi_i$  values with composition of NMP. This indicates the presence of intermolecular interactions between the component molecules of the mixture. In order to substantiate the presence of interactions (either adhesive or cohesive forces) between the molecules, it is essential to study excess parameters like excess free volume ( $_{V_{c}}^{E}$ ), excess internal pressure ( $\pi_{i}^{E}$ ), excess

molar available volume  $(V_a^E)$  etc., as these parameters are found to be more sensitive towards intermolecular interactions in the liquid mixtures [20].

In pure state, alkyl amines are weakly self-associated [8]. Although, the addition of a strongly polar solvent (NMP) disrupts the association of the amine, the increase in ultrasonic speed with NMP addition indicates strong interactions between the component molecules [16]. However, the excess functions are very constructive in understanding molecular interactions between components of liquid mixtures. By definition, the excess function  $Y^E$  represents the excess of a given quantity Y of a real mixture over its value for an ideal mixture  $Y^{id}$  at the same conditions of pressure, temperature, and composition [17]. When alkyl amines are added to NMP it results in considerable decrease in intermolecular spaces between molecules leading to decrease in free volume and hence increase in internal pressure. So negative values of  $V^E$  and positive  $\pi_i^E$  values

are observed in the present case. Our finding is in good agreement with the views proposed by Jacobson [21].

The  $V_f^E$  values are found to decrease (Table 2) with increase in the concentration of NMP,

attaining a minimum value between 0.4-0.5 mole fraction of NMP. This indicates that the associated structure of the polar component (NMP) due to dipolar association has been broken by solvent molecules. The negative  $V_f^E$  values indicate the contributions made by the strong dipole-

dipole interactions between the unlike molecules of the components [22].

**Table2.** Excess molar volumes  $(10^6 x V_m^E / m^3 \cdot mol^{-1})$  for the binary mixtures of N-methyl-2-pyrrolidone (NMP) and alkyl amines (PA or BA or DPA) at temperatures of 303.15, 308.15, 313.15 and 318.15 K

		NMP	+PA				NMP	+ BA			NMP + DPA			
x1	303.15 K	308.15 K	313.15 K	318.15 K	<b>X</b> 1	03.15 K	308.15 K	313.15 K	318.15 K	<b>x</b> <sub>1</sub>	303.15 K	308.15 K	313.15 K	318.15 K
0.0000	0.000	0.000	0.000	0.000	0.0000	0.000	0.000	0.000	0.000	0.0000	0.000	0.000	0.000	0.000
0.0873	-8.838	-9.316	-9.308	-9.655	0.1033	-7.555	-7.953	-7.654	-7.945	0.1370	-9.616	-12.901	-12.970	-14.740
0.1771	-11.942	-12.999	-12.621	-13.339	0.2059	-10.111	-10.608	-10.497	-10.939	0.2631	-12.389	-16.053	-16.256	-18.365
0.2695	-12.701	-13.884	-13.581	-14.415	0.3077	-10.516	-11.264	-11.286	-11.765	0.3797	-12.625	-16.133	-16.501	-18.553
0.3646	-12.271	-13.360	-13.244	-14.018	0.4087	- 10.059	-10.882	-10.895	-11.263	0.4878	-11.728	-14.784	-15.222	-17.079

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0.4626	-11.147	-12.298	-12.155	-12.890	0.5091	-9.049	-9.794	-9.816	-10.220	0.5882	-10.240	-12.795	-13.175	-14.775
0.5636	-9.613	-10.578	-10.462	-11.159	0.6087	-7.605	-8.205	-8.184	-8.516	0.6818	-8.349	-10.433	-10.747	-12.079
0.6676	-7.677	-8.443	-8.381	-8.939	0.7076	-5.806	-6.288	-6.321	-6.541	0.7692	-6.344	-7.928	-8.115	-9.195
0.7749	-5.404	-5.943	-5.886	-6.285	0.8057	-3.911	-4.244	-4.276	-4.427	0.8511	-4.305	-5.348	-5.441	-6.132
0.8857	-2.814	-3.142	-3.110	-3.354	0.9032	-2.033	-2.132	-2.169	-2.268	0.9278	-2.196	-2.701	-2.798	-3.109
1.0000	0.000	0.000	0.000	0.000	1.0000	0.000	0.000	0.000	0.000	1.0000	0.000	0.000	0.000	0.000



**Fig1.** Variation of internal pressure,  $\pi_i^E$ , for the binary mixtures NMP + PA or BA or DPA at 303.15 K aginst mole fraction of NMP

Excess values of  $\pi_i^E$  (Figure 1, Table 3) in the binary mixtures of NMP with PA or BA or DPA show a maximum value between 0.4-0.5 mole fraction of NMP, then decrease with further increase in its concentration. This indicates the weakening of intermolecular interaction between component molecules. Thus based on the magnitude of positive values in  $\pi_i^E$ , the order of the interaction, in the substituted benzenes under investigation at 308.15 and 318.15 K with NMP is as follows: PA > BA > DPA.

**Table3.** Excess internal pressures  $(10^8 x \pi_i^E / Pa)$  for the binary mixtures of N-methyl-2-pyrrolidone (NMP) and alkyl amines (PA or BA or DPA) at temperatures of 303.15, 308.15, 313.15 and 318.15 K

		NMF	P + PA				NMI	P + BA			NMP + DPA			
X1	303.15 K	308.15 K	313.15 K	318.15 K	$\mathbf{x}_1$	303.15 K	308.15 K	313.15 K	318.15 K	<b>x</b> <sub>1</sub>	303.15 K	308.15 K	313.15 K	318.15 K
0.0000	0.000	0.000	0.000	0.000	0.0000	0.000	0.000	0.000	0.000	0.0000	0.000	0.000	0.000	0.000
0.0873	0.420	0.387	0.384	0.363	0.1033	0.283	0.269	0.249	0.242	0.1370	0.175	0.160	0.152	0.154
0.1771	0.684	0.655	0.618	0.596	0.2059	0.451	0.422	0.403	0.392	0.2631	0.255	0.245	0.233	0.235
0.2695	0.830	0.799	0.757	0.732	0.3077	0.527	0.509	0.495	0.479	0.3797	0.301	0.297	0.288	0.287
0.3646	0.886	0.844	0.815	0.783	0.4087	0.558	0.549	0.529	0.502	0.4878	0.323	0.316	0.313	0.309
0.4626	0.868	0.848	0.810	0.778	0.5091	0.548	0.539	0.519	0.497	0.5882	0.322	0.313	0.308	0.305
0.5636	0.794	0.773	0.734	0.711	0.6087	0.492	0.481	0.458	0.437	0.6818	0.288	0.286	0.281	0.281
0.6676	0.661	0.641	0.611	0.591	0.7076	0.391	0.385	0.371	0.351	0.7692	0.240	0.243	0.232	0.240
0.7749	0.480	0.466	0.441	0.428	0.8057	0.273	0.270	0.262	0.248	0.8511	0.183	0.183	0.172	0.174
0.8857	0.256	0.254	0.242	0.239	0.9032	0.152	0.141	0.140	0.136	0.9278	0.105	0.103	0.104	0.101
1.0000	0.000	0.000	0.000	0.000	1.0000	0.000	0.000	0.000	0.000	1.0000	0.000	0.000	0.000	0.000

The presence of stronger interactions, are further substantiated by the negative values of  $V_a^E$  for these binary liquid mixtures. Molar available volume is a quantity which depends on the molecular packing of the systems. In the present investigation  $V_a^E$  values (Table 4) show negative/positive deviations, confirming that strong magnitude of interactive forces, existing

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between the unlike molecules of the component liquids in all the three binary systems, over the entire composition range of NMP.

**Table4.** Excess molar available volumes  $(10^6 x V_a^E / m^3 \cdot mol^{-1})$  for the binary mixtures of N-methyl-2pyrrolidone (NMP) and alkyl amines (PA or BA or DPA) at temperatures of 303.15, 308.15, 313.15 and 318.15 K

_		NMI	P + PA				NMP -	+ BA			NMP + DPA			
<b>x</b> <sub>1</sub>	303.15 K	308.15 K	313.15 K	318.15 K	<b>x</b> <sub>1</sub>	303.15 K	308.15 K	313.15 K	318.15 K	<b>x</b> <sub>1</sub>	303.15 K	308.15 K	313.15 K	318.15 K
0.0000	0.000	0.000	0.000	0.000	0.0000	0.000	0.000	0.000	0.000	0.0000	0.000	0.000	0.000	0.000
0.0873	0.119	0.050	-0.024	-0.108	0.1033	-0.199	-0.227	-0.258	-0.388	0.1370	-0.085	-0.027	-0.083	-0.151
0.1771	0.204	0.093	-0.043	-0.171	0.2059	-0.326	-0.378	-0.404	-0.584	0.2631	0.277	0.180	0.143	0.119
0.2695	0.261	0.106	-0.066	-0.220	0.3077	-0.395	-0.472	-0.528	-0.696	0.3797	0.593	0.543	0.529	0.508
0.3646	0.280	0.100	-0.104	-0.280	0.4087	-0.441	-0.519	-0.613	-0.824	0.4878	1.096	1.055	1.024	0.979
0.4626	0.276	0.071	-0.134	-0.308	0.5091	-0.448	-0.539	-0.622	-0.773	0.5882	1.675	1.553	1.578	1.519
0.5636	0.263	0.045	-0.128	-0.280	0.6087	-0.414	-0.504	-0.561	-0.722	0.6818	1.907	1.846	1.726	1.769
0.6676	0.256	0.070	-0.074	-0.207	0.7076	-0.348	-0.431	-0.488	-0.617	0.7692	1.881	1.846	1.746	1.736
0.7749	0.216	0.065	-0.050	-0.163	0.8057	-0.258	-0.326	-0.377	-0.449	0.8511	1.859	1.751	1.528	1.417
0.8857	0.133	0.050	-0.042	-0.108	0.9032	-0.133	-0.171	-0.217	-0.271	0.9278	1.275	1.189	1.110	0.928
1.0000	0.000	0.000	0.000	0.000	1.0000	0.000	0.000	0.000	0.000	1.0000	0.000	0.000	0.000	0.000

The values of the adjustable coefficients  $A_{j-1}$  of Redlich-Kister polynomial along with the standard deviations for excess free volume  $(V_f^E)$ , excess internal pressure  $(\pi_i^E)$ , and Molar available

volume  $(V_a^E)$  at temperatures 308.15 and 318.15 K are presented in Table 5.

**Table5.** Redlich-Kister Coefficients  $(A_{j-1})$  and the Standard Deviations  $(\sigma)$  of Excess Parameters for the Binary Mixture of NMP and PA or BA or DPA at Different Temperatures

	T/K	$\mathbf{A}_{0}$	A <sub>1</sub>	A <sub>2</sub>	A <sub>3</sub>	$A_4$	σ						
		N-methy	l-2-pyrrolidone(1)	+ propylamin	e(2)								
$V_f^E/10^{-6} \text{ m}^3 \text{ mol}$	303.15	-42.5886	-28.2808	-21.2032	-32.5488	-26.3877	0.086						
	308.15	-46.9471	-31.8241	-22.9947	-29.7823	-24.3426	0.047						
	313.15	-46.5280	-30.0274	-19.0381	-32.4394	-30.8042	0.103						
	318.15	-49.3061	-32.0825	-22.9595	-31.2905	-26.1733	0.067						
$\pi_{\rm s}^{\rm E}$ / 10 <sup>-8</sup> Pa <sup>-1</sup>	303.15	3.3824	1.3885	0.7003	0.4533	0.0181	0.001						
	308.15	3.3038	1.3984	0.4743	0.0584	0.0904	0.008						
	313.15	3.1608	1.2666	0.1676	0.3131	0.7014	0.002						
	318.15	3.0327	1.2414	0.4117	0.1463	0.2981	0.003						
N-methyl-2-pyrrolidone(1) + butylamine(2)													
$V_f^E/10^{-6} \text{ m}^3 \text{ mol}$	303.15	-36.6370	-23.9750	-13.1044	-20.2378	-19.0318	0.014						
	308.15	-39.6450	-25.2772	-12.7740	-21.2788	-18.8752	0.054						
	313.15	-39.7424	-25.9423	-13.6624	-16.5632	-13.6945	0.045						
	318.15	-41.3874	-27.5044	-13.6661	-16.1186	-14.9078	0.052						
$\pi_{\rm s}^{~{\rm E}}$ / 10 <sup>-8</sup> Pa <sup>-1</sup>	303.15	2.2070	0.6954	-0.2213	0.2245	0.8269	0.006						
	308.15	2.1667	0.6120	-0.3073	0.3147	0.7261	0.001						
	313.15	2.0869	0.6490	-0.1895	0.0569	0.4437	0.002						
	318.15	-3.1766	-0.9404	0.1029	0.5818	0.1890	0.010						
		N-methyl	-2-pyrrolidone(1) -	+ dipropylami	ne(2)								
$V_f^E/10^{-6} \text{ m}^3 \text{ mol}$	303.15	-46.3749	-25.4772	-14.9055	-14.1529	-11.5086	0.017						
	308.15	-58.2666	-34.8150	-26.0110	-22.0517	-12.3765	0.063						
	313.15	-59.9688	-35.0538	-22.7284	-20.9459	-15.4622	0.068						
	318.15	-67.1435	-39.4416	-30.2075	-24.9968	-12.2846	0.097						
$\pi_{s}^{E} / 10^{-8} Pa^{-1}$	303.15	1.3126	-0.1306	-0.1865	0.3043	0.8675	0.003						
	308.15	1.2734	-0.0888	0.1007	0.0383	0.2706	0.001						
	313.15	1.2598	-0.1125	-0.2198	0.0508	0.7190	0.002						
	318.15	1.2346	-0.1188	0.1619	0.0603	0.1621	0.003						

Increase in temperature causes variation in the excess thermodynamic properties as the local structure of the liquids are destroyed, thus affecting their intermolecular free length and kinetic

energy so the values of excess free volume  $(V_f^E)$ , excess internal pressure  $(\pi_i^E)$ , and excess molar

available volume  $(V_a^E)$  varies with temperature (Table 2). Similar temperature dependence results are reported earlier by several researchers [23,24].

### 4. CONCLUSIONS

From the observed thermo-acoustic and thermodynamic studies of the binary liquid mixtures of N-methyl-2-Pyrrolidone + Propylamine, + Butylamine, + Dipropylamine at different temperatures and at atmospheric pressure, it is clear that all the three binary systems exhibited non-linear increase /decrease in V<sub>f</sub>, and  $\pi_i$  values with the composition of NMP which indicate the presence of intermolecular interactions between the component molecules of the mixtures. The values of  $V_f^E$  for all the three binary mixtures are negative and the values of,  $\pi_i^E$  were positive over the entire range of composition of NMP and the temperatures under study. The observed thermoacoustic results suggest a strong interaction between the NMP and substituted benzene under study.

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